

# Poly(hydroxybutyrate) in Vivo: NMR and X-ray Characterization of the Elastomeric State

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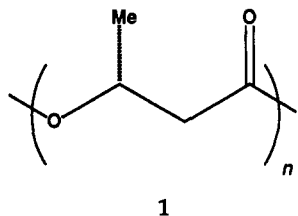
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**ABSTRACT:** Variable-temperature  $^{13}\text{C}$  NMR relaxation studies of whole cells of *Alcaligenes eutrophus* show that poly( $\beta$ -hydroxybutyrate) (PHB) is an amorphous elastomer in its "native" state within granules. The in vivo  $T_g$  is estimated to be around  $-40^\circ\text{C}$ . Rotational correlation times and Arrhenius and other kinetic parameters are all consistent with amorphous elastomers that have been well characterized as bulk polymers. X-ray powder diffraction patterns of whole cells confirm that essentially 100% of PHB in its native state is amorphous.

## Introduction

Poly(hydroxybutyrate) (PHB, 1) is a microbial storage polymer with intriguing properties. The isolated material



is highly crystalline, melting at  $173\text{--}180^\circ\text{C}$ , and with a glass transition temperature ( $T_g$ ) of  $9^\circ\text{C}$ ,<sup>1</sup> but in the live cell it is found in discrete granules whose physical properties have been the subject of much discussion. Electron microscopy<sup>2</sup> and CPMAS<sup>3,4</sup> NMR studies of isolated and dried granules indicated the presence of highly crystalline structures, which were assumed to be present also in native granules. This interpretation, while apparently providing a satisfactory physical description of granule structure, created a problem in understanding how the depolymerase enzyme could work so efficiently on a solid crystalline substrate. This conflict remained unsolved for many years.

Recent work in this laboratory<sup>5,6</sup> showed that, contrary to earlier belief, PHB is in a predominantly "mobile" state within the granules. Our conclusion was based on the observation of high-resolution  $^{13}\text{C}$  NMR spectra of PHB using solution techniques on live cells of *Alcaligenes eutrophus* and two *Methylobacterium* species. The frequency of local molecular motions required to give such sharp resonances are of the order of  $10^7\text{ s}^{-1}$ . The  $^{13}\text{C}$  NMR properties over the temperature range  $10\text{--}30^\circ\text{C}$  matched qualitatively those expected of an amorphous polymer above its  $T_g$ : the observed small NOE for main-chain carbons, longer  $T_1$ s at lower temperatures, and dramatic broadening of the signals over a small temperature range are well-documented features of such elastomeric polymers.<sup>7</sup> We also showed that treatments of the kind used to prepare isolated granules for spectroscopy can lead to solidification of the PHB to give the crystalline structures previously observed.

We now report detailed  $^{13}\text{C}$  NMR measurements of PHB in its native state over a much larger temperature range and at two different field strengths. By fitting the relaxation parameters to a detailed model and comparison

with well-characterized bulk synthetic polymers, we show that the physical properties of PHB in submicron granules are consistent with those of a bulk elastomer with  $T_g$  of around  $-40^\circ\text{C}$ . Furthermore we have used X-ray powder diffraction of whole cells to demonstrate the absence of significant amounts of crystalline material. We shall discuss elsewhere the mechanism of PHB plasticization in vivo.

## Theory

We consider only amorphous polymers well above their  $T_g$ ; molecular motion in such materials is sufficiently fast to give sharp spectra by averaging carbon-proton dipolar couplings and chemical shift anisotropies. Below  $T_g$ , molecular motion even in amorphous regions is too slow. Then solid-state NMR techniques such as CPMAS have to be used.<sup>7</sup>

Relaxation studies<sup>7</sup> of amorphous elastomers above  $T_g$  generally assume that, in common with isotropic rotational diffusion in solution, the correlation time associated with the motion of the CH vector ( $\tau_c$ ) is dependent on temperature and follows an Arrhenius relationship:

$$\tau_c = \tau_c^\circ \exp(-E_a/RT) \quad (1)$$

where  $E_a$  is an activation energy for the rotation. The various models of polymer motion and the above assumption are used to predict how the relaxation parameter should vary with temperature. The predicted curves are fitted to the relaxation data by varying the parameters of the model, the preexponential factor ( $\tau_c^\circ$ ), and  $E_a$ . We have proceeded in a slightly different manner. We have assumed a simple model from which, given a  $T_1$  value, we can obtain an estimate of  $\tau_c$ . Plots of  $\ln \tau_c$  against inverse temperature have allowed the calculation of a value for the activation energy of the barrier to the motion causing  $T_1$  relaxation and this has been compared to those found for bulk synthetic elastomers.

Assuming that carbon relaxation occurs purely by the  $^{13}\text{C}\text{--}^1\text{H}$  dipolar relaxation mechanism, the spin-lattice relaxation time ( $T_1$ ), the spin-spin relaxation time ( $T_2$ ) and NOE are given by the well-known expressions<sup>8</sup>

$$\frac{1}{T_1} = \frac{h^2 \gamma_C^2 \gamma_H^2}{40\pi^2} \sum_i r_i^{-6} [J(\omega_H - \omega_C) + 3J(\omega_C) + 6J(\omega_H + \omega_C)] \quad (2)$$

$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{h^2 \gamma_C^2 \gamma_H^2}{80\pi^2} \sum_i r_i^{-6} [4J(0) + 6J(\omega_H)] \quad (3)$$

$$\text{NOE} = 1 + \frac{\gamma_H}{\gamma_C} \left[ \frac{6J(\omega_H + \omega_C) - J(\omega_H - \omega_C)}{J(\omega_H - \omega_C) + 3J(\omega_C) + 6J(\omega_H + \omega_C)} \right] \quad (4)$$

where  $\gamma_C$  and  $\gamma_H$  are the carbon and proton gyromagnetic ratios, respectively;  $\omega_C$  and  $\omega_H$  are the corresponding resonance frequencies,  $r_i$  is the distance between the  $^{13}\text{C}$  nucleus of interest and the  $i$ th relaxing proton, and  $J(\omega_i)$  is the spectral density function. Normally for  $T_1$  measurements, only directly bonded protons (with bond length  $r_{\text{CH}}$ ) are considered—the  $r^{-6}$  dependence of dipole–dipole interactions ensures that their influence far outweighs any other protons. Therefore,  $^{13}\text{C}$   $T_1$ s are roughly proportional to the inverse of the number of bound protons for a given value of  $\tau_C$ . The spectral density functions are Fourier transforms of the autocorrelation functions of second-order spherical harmonics. They describe the power available at angular frequency  $\omega_i$  from the fluctuating interaction. The form of  $J(\omega_i)$  depends on the model used to describe the molecular motion.

The simplest model generally used is that of isotropic rotational diffusion, where  $J(\omega_i)$  has the following form:

$$J(\omega_i) = \tau_C / (1 + \omega_i^2 \tau_C^2) \quad (5)$$

A major drawback of the simple isotropic model with respect to polymers is its inability to predict correctly the value of the  $T_1$  minimum. More complicated models incorporating segmental motions involving several,<sup>9</sup> or a distribution of, correlation times<sup>10</sup> or librational motions<sup>11</sup> have been invoked to account for the discrepancies between the experimental  $T_1$ s and those predicted by the isotropic model. All these models incorporate longer correlation times to account for the observation of smaller NOEs and larger line widths than expected at high temperatures. For example, Howarth<sup>12</sup> measured the temperature dependence of  $^{13}\text{C}$   $T_1$ s and NOEs for natural rubber. He argued that the  $^{13}\text{C}$   $T_1$ s could not be fitted simultaneously to experimental values at both the  $T_1$  minimum and high temperature by use of models involving only isotropic reorientations. The data were, however, consistent with a three-correlation-time model or a combined fast anisotropic libration and reptation (looping motion) model. The three-correlation-time model involved a relatively slow isotropic motion, a slightly faster anisotropic motion, considered as a libration, and a fast anisotropic libration.

Dejean et al.<sup>13</sup> combined the conformational jump model of Hall and Helfand<sup>9</sup> with fast anisotropic librations to model accurately the  $^{13}\text{C}$   $T_1$  variation of poly(vinyl methyl ether) with temperature at 62 and 25 MHz. We have adopted their approach as it is relatively simple and allows comparisons to be made both with the relaxation behavior of other amorphous elastomers and with PHB in tetrachloroethane solution.<sup>14</sup> The real part (Re) of the spectral density function for the Hall–Helfand (HH) model can be written as

$$J(\omega) = \text{Re} [1/[(\alpha + i\beta)^{1/2}]] \quad (6)$$

where  $\alpha = \tau_2^{-2} + 2\tau_1^{-1}\tau_2^{-1} - \omega^2$ ,  $\beta = -2\omega(\tau_1^{-1} + \tau_2^{-1})$ .  $\tau_1$  is the correlation time for the cooperative or correlated jumps responsible for orientation diffusion along the chain and  $\tau_2$  corresponds to damping either by nonpropagative specific single conformational transitions or by distortions of the chain with respect to its most stable conformation.

The correlation times,  $\tau_1$  and  $\tau_2$ , can have different activation energies, which are associated with their different motions.

Dejean et al.<sup>13</sup> made the simplifying approximation that the ratio  $\tau_2/\tau_1$  remains constant, in effect giving  $\tau_2$  and  $\tau_1$  the same activation energy but a different preexponential constant. For ratios  $\tau_2/\tau_1$  between 2 and 10, this model gives  $T_1$  values slightly different from the isotropic model for a given  $\tau_1$ . For  $\tau_2/\tau_1$  greater than 10, the HH model diverges significantly from the isotropic model only at correlation times shorter than  $10^{-9}$  s, giving lower values of  $^{13}\text{C}$   $T_1$  for a given  $\tau_1$ . The value of  $\tau_2/\tau_1$  was found to be invariant when values of  $T_1$  were fitted against temperature for poly(vinyl methyl ether) in the bulk amorphous solid or in chloroform solution.<sup>13</sup> A recent study of PHB relaxation in tetrachloroethane solution using this approach gives an optimum  $\tau_2/\tau_1$  ratio of around 3.<sup>14</sup>

A fast anisotropic libration causes the value of the  $T_1$  minimum to be increased by an amount dependent on the angle of libration. The spectral density of a model combining the HH model and fast anisotropic bond librations can be written<sup>13</sup> as

$$J(\omega) = \frac{1-a}{(\alpha + i\beta)^{1/2}} + \frac{a\tau_0}{(1 + \omega^2\tau_0^2)} \quad (7)$$

so long as  $\tau_0 \ll \tau_1$ ; where  $\alpha = \tau_2^{-2} + 2\tau_1^{-1}\tau_2^{-1} - \omega^2$ ,  $\beta = -2\omega(\tau_1^{-1} + \tau_2^{-1})$ ,  $\tau_1$  and  $\tau_2$  have the same physical meaning as above,  $\tau_0$  is the correlation time associated with the libration motion, and  $(1-a)^{1/2} = (\cos \theta - \cos^3 \theta)/(2 - 2 \cos \theta)$ , where  $\theta$  is the conic half-angle for libration. Designating

$$J_{\text{HH}}(\omega) = 1/[(\alpha + i\beta)^{1/2}]$$

and

$$J_0(\omega) = \tau_0 / (1 + \omega^2\tau_0^2)$$

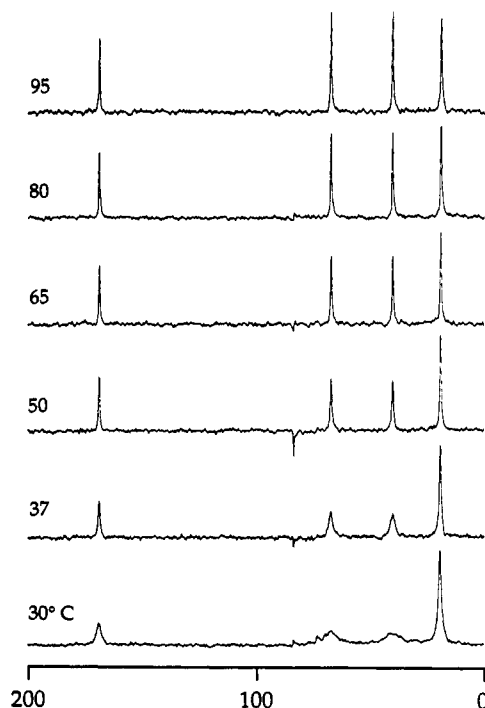
this allows  $T_1^{-1}$  to be written as the sum of two terms:

$$\begin{aligned} \frac{1}{T_1} = (1-a) \frac{h^2 \gamma_C^2 \gamma_H^2}{40\pi^2} r_{\text{CH}}^{-6} [J_{\text{HH}}(\omega_H - \omega_C) + 3J_{\text{HH}}(\omega_C) + \\ 6J_{\text{HH}}(\omega_H + \omega_C)] + a \frac{h^2 \gamma_C^2 \gamma_H^2}{40\pi^2} r_{\text{CH}}^{-6} [J_0(\omega_H - \omega_C) + \\ 3J_0(\omega_C) + 6J_0(\omega_H + \omega_C)] \quad (8) \end{aligned}$$

If  $(\omega_H + \omega_C)\tau_0 \ll 1$ , then the second term can be neglected and  $T_1$  is lengthened by a factor of  $1/(1-a)$ .

Howarth<sup>12</sup> and Dejean et al.<sup>13</sup> set  $(1-a)$  so that the theoretical  $T_1$  matches the experimental  $T_1$ ; the value of  $\theta$  can then be calculated by solving the cubic equation in  $\cos \theta$ . Dejean et al. set the ratio  $\tau_1/\tau_0$  to be constant and sufficiently large that  $(\omega_H + \omega_C)\tau_0 \ll 1$  throughout the temperature range. The second term of the above equation can be neglected, and the  $T_1$  minimum is then approximately equal to the  $T_1$  minimum of the HH model multiplied by  $1/(1-a)$ . This assumes that the activation energy of libration motion is the same as that for the  $\tau_1$  motion. While it seems likely that  $\tau_1$  and  $\tau_2$  have activation energies of the same order (For PHB in tetrachloroethane solution,  $E_a$  for  $\tau_1$  and  $\tau_2$  are 22 and 42 kJ mol<sup>-1</sup>, respectively.), it appears unlikely that  $E_a$  for the libration will be the same also. Howarth noted that wide variation in his fast libration correlation time had little effect on the relaxation parameters and set it to a fixed value.<sup>11</sup>

If the correlation time  $\tau_1$  follows an Arrhenius relationship, then a plot of  $\ln \tau_1$  against inverse temperature should yield a straight line whose gradient is  $-E_a/R$ . On the other hand,  $\tau_1$  in bulk polymers tends to follow the



**Figure 1.** 100-MHz natural-abundance  $^{13}\text{C}$  spectra of suspensions of *A. eutrophus* cells at various temperatures. Each spectrum is the result of acquiring 200 transients.

Williams-Landel-Ferry (WLF) equation.<sup>15</sup> This empirical relationship gives the ratio of the  $\tau_1$  at a temperature  $T$  to that of a reference temperature (usually taken as  $T_g$ ) for a polymer in the range  $T_g$  to around  $T_g + 100$ :

$$\log \left( \frac{\tau_c(T)}{\tau_c(T_{\text{ref}})} \right) = \frac{-C_1(T - T_{\text{ref}})}{C_2 + (T - T_{\text{ref}})} \quad (9)$$

$C_1$  and  $C_2$  are arbitrary factors that vary according to the reference temperature chosen. With  $T_{\text{ref}} = T_g$ ,  $C_1$  and  $C_2$  were at first thought to be universal constants, but they have since been shown to vary slightly from polymer to polymer;<sup>16</sup> they fall in the small range 11–17 for  $C_1$  and 40–70 for  $C_2$  except for polyisobutylene, which has an abnormally high value of  $C_2$ . While it is obviously impossible for the correlation time simultaneously to satisfy both an Arrhenius ( $1/T$ ) and WLF ( $T$ ) dependence on temperature, experimental error and small temperature range available often preclude distinction between these two mathematical models. In common with others,<sup>17</sup> we will show that our data are consistent with both models.

## Results and Discussion

**Temperature Dependence of  $^{13}\text{C}$  Spectra.** Figure 1 shows 100-MHz proton-decoupled  $^{13}\text{C}$  spectra of stationary-phase *A. eutrophus* cells over the temperature range 30–95 °C. Each spectrum is the result of collecting 200 transients; 10-s relaxation delays were allowed between acquisitions to ensure reliable peak intensities to be observed. The most striking features of this series of spectra are (a) that PHB is the only species detected, a measure of the huge internal concentration of mobile polymer within the cell, and (b) the variation in the relative heights of the carbon signals. All the temperature-dependent features of these spectra are fully reversible. While heat-treated cells are clearly not viable, there are no irreversible changes detected in the spectroscopic properties of the granules within these cells.

These variations are easily interpreted qualitatively. At 30 °C, the methyl carbon resonance is receiving almost its

**Table I**  
Temperature Dependence of Line Widths of Native PHB at 100.1 MHz

temp, °C	line width at 100.1 MHz, Hz			
	CO	CH	CH <sub>2</sub>	CH <sub>3</sub>
30	250	>400	>400	110
37	100	220	280	70
50	50	65	70	40
65	35	35	40	30
80	30	30	30	30
95	30	30	30	30

**Table II**  
Temperature Dependence of Line Widths of Native PHB at 62.9 MHz

temp, °C	line width at 62.9 MHz, Hz			
	CO	CH	CH <sub>2</sub>	CH <sub>3</sub>
30	80	>250	>250	70
40	25	40	45	15
50	15	20	25	10
65	15	15	25	10
80	15	15	15	10

**Table III**  
Temperature Dependence of  $T_1$  of Native PHB at 100.1 MHz

temp, °C	$T_1$ at 100.1 MHz, s			
	CO	CH	CH <sub>2</sub>	CH <sub>3</sub>
30	8.2	1.4	0.53	0.62
37	5.3	0.90	0.36	0.57
50	2.5	0.45	0.24	0.55
65	1.4	0.30	0.16	0.58
80	1.3	0.30	0.18	0.65
95	1.9	0.34	0.23	0.98

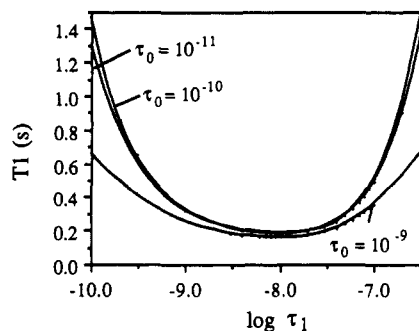
full NOE and is relatively sharp as a result of fast internal rotation about the methyl-methine bond. Only the much slower overall reorientation of the polymer backbone is available to the methylene and methine carbons, so their resonances are broad and lack the NOE. By 50 °C, faster backbone motion has dramatically sharpened the methylene and methine signals but not yet brought the NOE into action; the methyl carbon resonance is about twice the height of the other carbon signals. At 95 °C, the methylene and methine signals are roughly the same intensity as the methyl signal because faster overall reorientations of the polymer backbone at higher temperature have increased their NOEs substantially and sharpened the signals. These line-width results are summarized in Table I. Qualitatively similar results at 62.9 MHz are given in Table II.

These results confirm our earlier observations and conclusions but do not allow quantitative comparison with well-characterized bulk polymers. For this we turned to relaxation times.

**Temperature Dependence of  $^{13}\text{C}$  Relaxation Times.** Spin-lattice relaxation times were measured at 100 MHz by saturation-recovery over the temperature range 30–95 °C. The results are summarized in Table III and were used to fit the above model as described below. Subsequently, further experiments were carried out at 62.9 MHz to test our predictions of methylene and methine carbon relaxation rates; these experimental results are given in Table IV. It is clear that the backbone carbons pass through the  $T_1$  minimum around 65 °C. It is also qualitatively clear that the methylene/methine relaxation rate ratio, which ranges from 1.5 to 2.6, is close to 2, as would be expected if their relaxation were induced by effectively the same molecular motion.

**Table IV**  
Temperature Dependence of  $T_1$  of Native PHB at 62.9 MHz

temp, °C	$T_1$ at 62.9 MHz, s			
	CO	CH	CH <sub>2</sub>	CH <sub>3</sub>
30		0.48	0.20	0.47
40	2.1	0.21	0.11	0.49
50	1.8	0.17	0.10	0.46
65	1.5	0.19	0.10	0.49
80	1.5	0.19	0.10	0.50
90	1.6	0.30	0.16	0.79



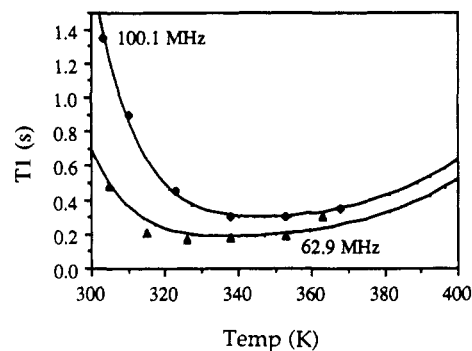
**Figure 2.** Calculated dependence of  $T_1$  on  $\tau_0$  and  $\tau_1$ .

The variation of the methyl  $T_1$  is significantly different from the backbone carbons. The  $T_1$  minimum is broader than those of the backbone carbons and is displaced to lower temperature because internal rotation is the major motion causing dipolar relaxation at low temperature. At high temperature this motion is too fast for efficient relaxation and the  $T_1$  rapidly increases. We have not modeled the relaxation of this group as this would not add much to our understanding of the overall motional properties of PHB.

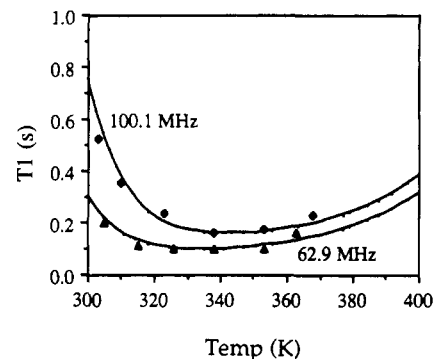
**Modeling the Molecular Motion of Native PHB.** At 95 °C the  $T_1$ s of the methine and methylene carbons have increased by less than 20% and 50%, respectively, of their minimum values. By use of the HH model and a value of 20 for the ratio  $\tau_2/\tau_1$ , the correlation time  $\tau_1$  varies between approximately  $10^{-6}$  and  $10^{-9}$  s. This is relatively insensitive to the  $\tau_2/\tau_1$  ratio in this temperature range: with the HH model, the predicted  $^{13}\text{C}$   $T_1$  at 100.1 MHz of the methine carbon is increased from 170 (isotropic model) to 210 ms (HH model;  $\tau_2/\tau_1 = 20$ ). The experimental value is 300 ms, and no matter how large the  $\tau_2/\tau_1$  ratio the Hall-Helfand model alone cannot predict a minimum that is this large.

Adding in the librational motions, we find (Figure 2) that variation of fixed  $\tau_0$  makes little difference to the  $T_1$  relaxation around the  $T_1$  minimum so long as  $\tau_0 < 10^{-10}$ . Therefore, we set  $\tau_0$  arbitrarily to  $10^{-11}$  s and varied the value of  $(1-a)$  so that the theoretical  $T_1$  minimum matched the experimental minimum. The fixed parameters used for modeling  $^{13}\text{C}$   $T_1$ s of the methine and methylene carbons are  $\tau_2/\tau_1 = 20$ ,  $\tau_0 = 10^{-11}$  s, CH bond length 1.09 Å. For the methine carbon, the best fit at 100 MHz (Figure 3) was obtained with  $(1-a) = 0.72$ , and for the methylene carbon (Figure 4)  $(1-a) = 0.67$ . Calculation gives half-conic angles of libration of 26° and 29°, respectively, values that are very similar to the recent estimate of 22° and 29° for PHB in solution.<sup>14</sup> The lower value for methine carbons has been observed in many polymers and has been attributed to greater steric hindrance at the methine carbon.<sup>12,13,18</sup>

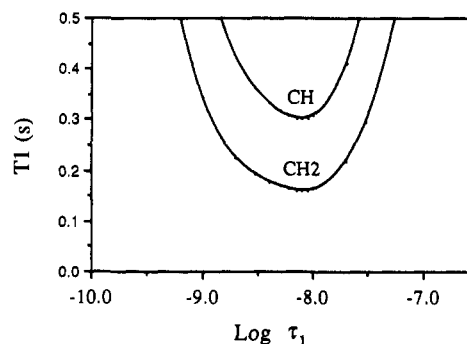
The predicted dependence of  $T_1$  on  $\log \tau_1$  at 100.1 MHz based on the above assumptions for both the methine and methylene carbons is given in Figure 5. The slightly different values for  $(1-a)$  are reflected in the fact that



**Figure 3.** Temperature dependence of the methine carbon  $T_1$  at 100 (●) and 62.9 MHz (▲). Curves are the best fit from the parameters given in the text.



**Figure 4.** Temperature dependence of the methylene carbon  $T_1$  at 100 (●) and 62.9 MHz (▲). Curves are the best fit from the parameters given in the text.



**Figure 5.** Predicted  $\tau_1$  dependence of methylene and methine carbon  $T_1$  at 100 MHz from the best-fit parameters.

the ratio of methine  $T_1$ /methylene  $T_1$  at the  $T_1$  minimum is somewhat less than 2.<sup>1</sup> Using the model outlined above (eq 8) and the values for the parameters  $\tau_2/\tau_1$ ,  $(1-a)$ , and  $\tau_0$  obtained by fitting it to the experimental  $T_1$ s at 100.1 MHz, we predicted the  $^{13}\text{C}$   $T_1$ s of the methine and methylene carbon at 62.9 MHz as a function of temperature. This required also using the values for the preexponential term ( $\tau_1^0$ ) and  $E_a$  obtained from the Arrhenius plot (see below). The theoretical curves for the  $^{13}\text{C}$   $T_1$ s and experimental data for both methine and methylene groups are shown in Figures 3 and 4. The parameters and model give a prediction that fits all the  $T_1$  data within experimental error.

**Arrhenius Behavior.**  $\log \tau_1$  values at a particular temperature were obtained directly from comparison of the experimental  $T_1$  values with the theoretical curves of Figure 5. The resulting Arrhenius plot is given in Figure 6 and show that, within experimental error,  $\tau_1$  does follow an Arrhenius relationship. The plots for both methine and methylene carbons yield activation energies that are essentially the same at  $E_a = 57 \pm 5 \text{ kJ mol}^{-1}$ . The ratio

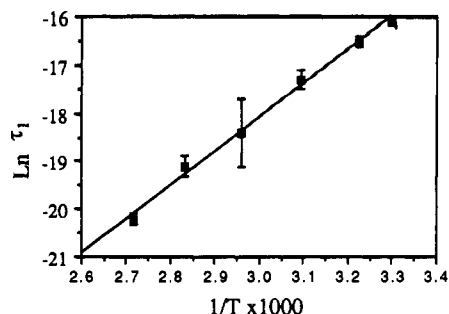


Figure 6. Arrhenius plot for the methine carbon.

Table V  
Activation Energies for Motion of Bulk and Dissolved Polymers

polymer	$E_{\text{act}}$ in soln, $\text{kJ mol}^{-1}$	$E_{\text{act}}$ in bulk, $\text{kJ mol}^{-1}$
poly(vinyl methyl ether) <sup>13</sup>	15	39
poly(propylene oxide) <sup>18</sup>		49
poly(ethylene oxide)		49
PHB	19.5 <sup>14</sup>	57 <sup>a</sup>

<sup>a</sup> This work.

$\tau_2/\tau_1$  has little effect on the value of  $E_a$ : with  $\tau_2/\tau_1 = 1$ ,  $E_a = 52 \text{ kJ mol}^{-1}$ . This is of the same order as the reported activated energies of other amorphous polymers in bulk. Table V gives the literature values<sup>13,14,18</sup> for the activation energy of  $\tau_1$  for various polymers in bulk amorphous solid or in solution. The activation energy ( $E_a$ ) can be thought of as being made up of two terms:<sup>19</sup>

$$E_a = E_\eta + E^* \quad (10)$$

where  $E_\eta$  is the activation energy required to overcome the viscosity of the solvent and  $E^*$  is the activation energy for the potential barrier of the local motion in the gas phase. Dais et al.<sup>14</sup> calculated that  $E^* \approx 8 \text{ kJ mol}^{-1}$  for PHB in solution. Assuming the same value  $E^*$  for PHB in the native state, this gives  $E_\eta \approx 50 \text{ kJ mol}^{-1}$  and confirms the importance of intermolecular interactions in bulk polymers found for poly(vinyl methyl ether).<sup>13</sup>

**Williams-Landel-Ferry Behavior.** In order to obtain values for the WLF constants we have estimated  $T_g$  by using the empirical relationship  $T_c/T_g \approx 1.2\text{--}1.3$  found by Dekmezian,<sup>17</sup> where  $T_c$  is the lowest temperature at which high-resolution spectra can be obtained by solution techniques. Again polyisobutylene is an exception, with  $T_c/T_g = 1.4$ . Clearly  $T_c$  is dependent on the resonance observed (being lower for more mobile side-chain resonances than backbone resonances), the instrumentation involved, and the experimental procedure. However, a rough estimate is all that is required for the purpose of seeing if  $\tau_1$  obeys WLF kinetics. For PHB in its native state  $T_c \approx 290 \text{ K}$ , which gives values of  $T_g$  in the range 220–240 K. We have used a value of  $T_g = 230 \text{ K}$  to plot  $(T - T_g)$  against  $-(T - T_g)/\ln \tau_1$  for the methine carbon (Figure 7). This gives values of  $C_1 = 12 \pm 1$  and  $C_2 = 51 \pm 10$  (errors estimated by taking values of  $T_g = 230 \pm 10 \text{ K}$ ), which are clearly within the range found for most bulk amorphous polymers (Table VI).

**X-ray Diffraction.** The experiments above have shown that most native PHB is amorphous and mobile, but have not demonstrated the absence of crystalline material. However, the large weight fraction of PHB present even under in vivo conditions allows X-ray diffraction to be used to estimate the proportion of crystalline material.

Table VI  
Values of  $C_1$  and  $C_2$  for Bulk Elastomers<sup>17</sup>

polymer	$C_1$	$C_2$
ethylene-propylene (62% Pr)	15.4	67.7
cis-polyisoprene	15.0	68.7
polyisobutylene	14.1	91.5
poly(vinyl acetate)	15.1	62.0
poly(isopropyl acrylate)	12.2	53.6
cis-polybutadiene	15.1	54.3
atactic polypropylene	15.2	60.7
native-state PHB <sup>a</sup>	12.0	51

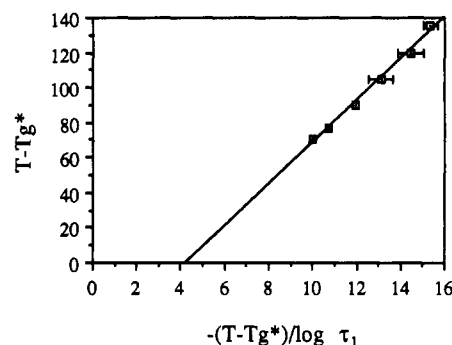
<sup>a</sup> This work.

Figure 7. WLF plot for the methine carbon.

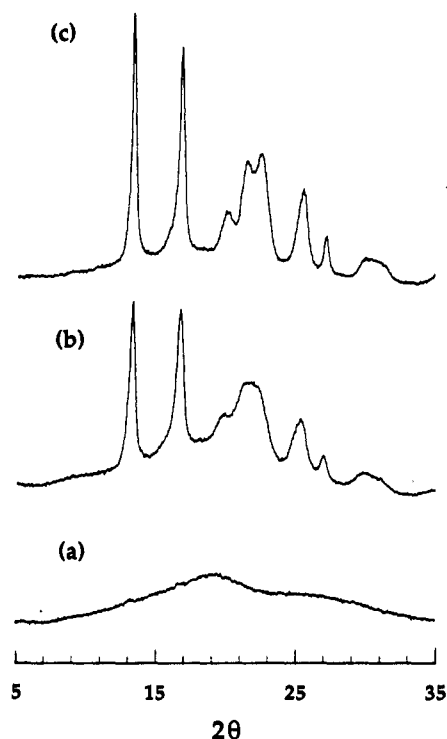


Figure 8. X-ray powder diffraction patterns for (a) a wet paste of *A. eutrophus* cells containing ca. 50% PHB by dry weight, (b) *A. eutrophus* cells that have been washed with acetone and dried (110 °C, 1 h), and (c) dry aqueously purified PHB.

Figure 8a shows that the X-ray powder diffraction pattern for a wet paste of *A. eutrophus* displays almost no features due to crystalline material. In contrast, when a sample of the same culture is washed in acetone and dried at 100 °C for 1 h a sharp diffraction pattern is observed (Figure 8b). This pattern is very similar to that of aqueously purified PHB (Figure 8c), whose crystal structure is well-known.<sup>20</sup>

We used the diffraction intensity to obtain quantitative estimates of crystallinity in these samples. In the diffraction pattern of "pure" PHB is seen a broad background

that arises from scattering by an amorphous component in the solid; the relative areas of the crystalline and amorphous diffraction patterns give an estimate of 65% crystallinity within this sample. In order to estimate the crystalline fraction of PHB within the wet-paste whole cells only the intensity of the strongest (020) reflections has been used, and absorption corrections have been made for the presence of water and other material. When these corrections have been made, a value of not more than 2% crystallinity is obtained, at the very limit of detection. If real, this crystallinity is probable produced by drying of cells at the surface of the sample. Thus in vivo X-ray diffraction shows that PHB in its native state is essentially all amorphous.<sup>21</sup>

## Conclusions

We have shown that the relaxation behavior of PHB in its native state is typical of an amorphous elastomer above its  $T_g$ . Overall segmental molecular motion is the dominant cause of longitudinal relaxation, although the rate of such motion is much slower than in solution. The activation energy for the process causing  $T_1$  relaxation in the native state is larger than for PHB in solution and is of the same magnitude as other bulk elastomers. Whole-cell X-ray diffraction shows that PHB in its native state is essentially all amorphous.

Strictly speaking, one cannot conclude that the model we have used, or any other model, necessarily elucidates the actual motions executed by the polymer chains. Any of the available models could probably be fitted to the methine and methylene  $^{13}\text{C}$   $T_1$  data that we obtained from native-state PHB; nevertheless, it is noteworthy that the model we have used gives essentially the same values for librational excursions as is observed by Dais et al. for PHB in solution.<sup>14</sup>

The immediate aim of this work has been to show that the mobility and relaxation properties of native PHB match those of synthetic polymers, which can be studied in bulk. More generally, these experiments are a powerful illustration of the power of whole-cell NMR, allowing the bulk properties of the polymer to be obtained from sub-micron particles within a cell.

While these results give a good description of the PHB in native granules, they do not explain how bacteria are able to store a crystalline polymer as a mobile elastomer. We previously suggested that the PHB in the granules is plasticized by water.<sup>6</sup> Elsewhere we present evidence to support this idea and show that another plasticizing agent may also be required to explain the mobility.<sup>22</sup>

## Experimental Section

Rich medium contained yeast extract (Oxoid L-21, 10 g/L), bacteriological peptone (Oxoid L-37, 10 g/L), Lab-lemco (Oxoid L-29, 5 g/L), fructose (10 g/L), and NaCl (5 g/L), pH 6.6. Minimal medium contained phosphate buffer (20 mL/L of stock  $\text{NaH}_2\text{PO}_4$  (72 g/L),  $\text{K}_2\text{HPO}_4$  (95 g/L)), ammonium sulfate (1.8 g/L), magnesium sulfate (0.2 g/L), and trace elements (6 mL/L of stock  $\text{CaCl}_2$  (5.2 g/L),  $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$  (0.08 g/L),  $\text{MnSO}_4 \cdot 4\text{H}_2\text{O}$  (0.04 g/L), and  $\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$  (0.04 g/L)). All media were sterilized by autoclaving for 20 min at 115 °C and 121 psi before use.

*Alcaligenes eutrophus* H16 (a naturally selected high-yielding strain supplied by ICI Biological Products, Billingham, UK) were grown on rich medium (500 mL) in 2-L shake flasks at 30 °C in an orbital incubator at 100 rpm. Cells were harvested when they reached an O.D.<sub>610</sub> of approximately 1. They were then centrifuged at 4000g for 10 min and resuspended in minimal medium (500 mL) in 2-L shake flasks containing fructose (10 g/L) as the sole carbon source. They were incubated for 48 h at 100 rpm and 30 °C.

Bacteria were centrifuged for 10 min at 4000g and 4 °C. The soft pellet was washed and finally taken up in a minimal volume of isotonic saline. This suspension (0.5 mL) was placed in a 5-mm NMR tube. A sealed capillary of deuterated benzene or (above 70 °C) deuterated 1,2-tetrachloroethane in the center of the NMR tube acted as lock signal and chemical shift reference.

Carbon spectra at 100.1 and 62.9 MHz were taken on Bruker AM 400 and WH 250 spectrometers, respectively. Waltz-16 broad-band decoupling was used, the sweep width was 220 ppm, and 8192 data points were collected. A 90° pulse length was used and the delay time between pulses was 5 s. A total of 200 transients were collected.

$T_1$ s of native PHB were measured by using saturation-recovery. The initial delay of the 90° pulse train was 200 ms; this was successively halved to  $\approx 1$  ms. Twelve interleaved variable delays, allowing  $T_1$  relaxation, between 10 ms and 10 s were used. The same acquisition parameters as above were used and 64 transients were acquired. No relaxation delay between pulse sequences is required.

X-ray diffraction data were collected on a Philips PW1710 ( $\theta$ - $2\theta$ ) diffractometer using Cu K $\alpha$  radiation ( $\lambda = 1.5418$  Å). Samples were placed in a constant-volume sample holder, which allowed a determination of the density ( $\rho$ ), and hence absorption coefficient, of the sample.

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